

Fault Tolerant Control

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Outline

- Definition of problem
- Modelling
- Fault detection filters
- Fault tolerant control systems
- Example

Introduction

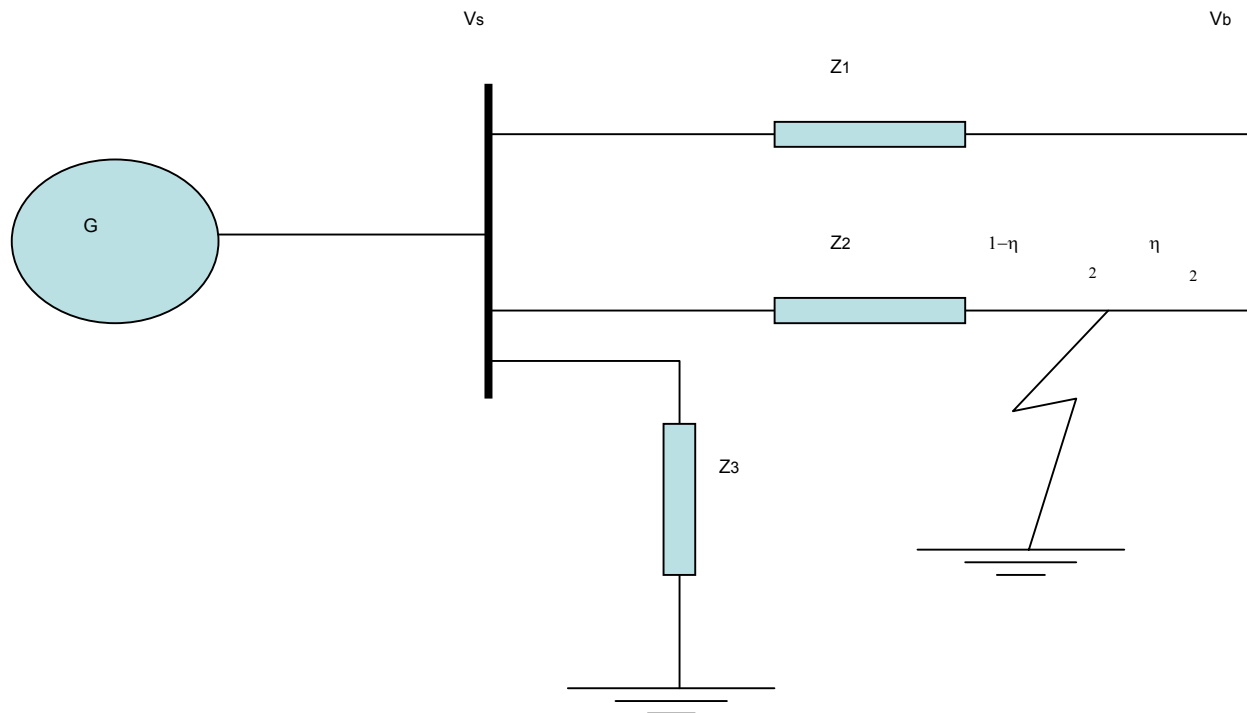
- Used in critical applications where faults cannot be tolerated
- Additional features need to be incorporated into the control system to maintain adequate/safe operation during abnormal conditions

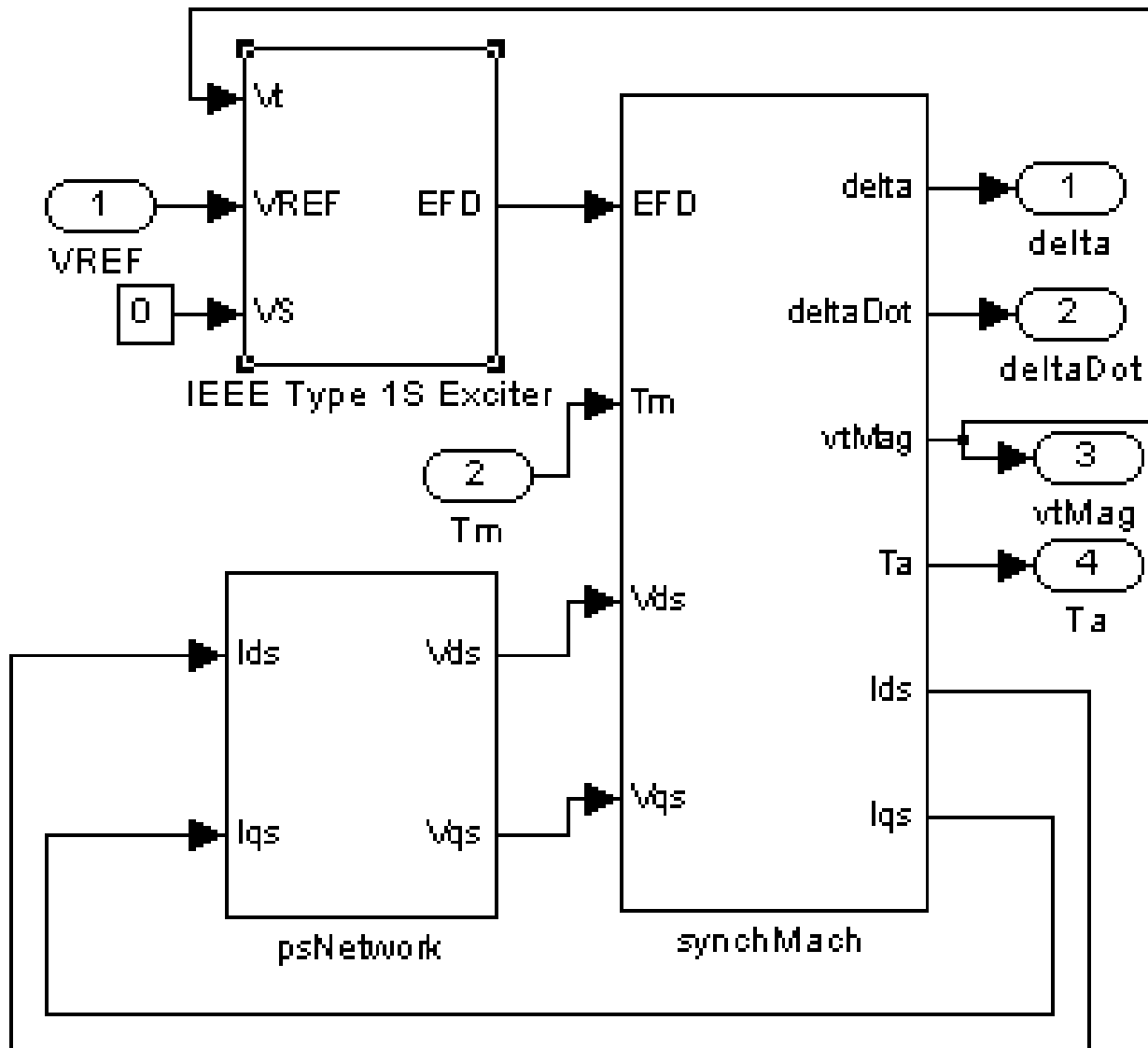
Example 1 – Fighter Aircraft

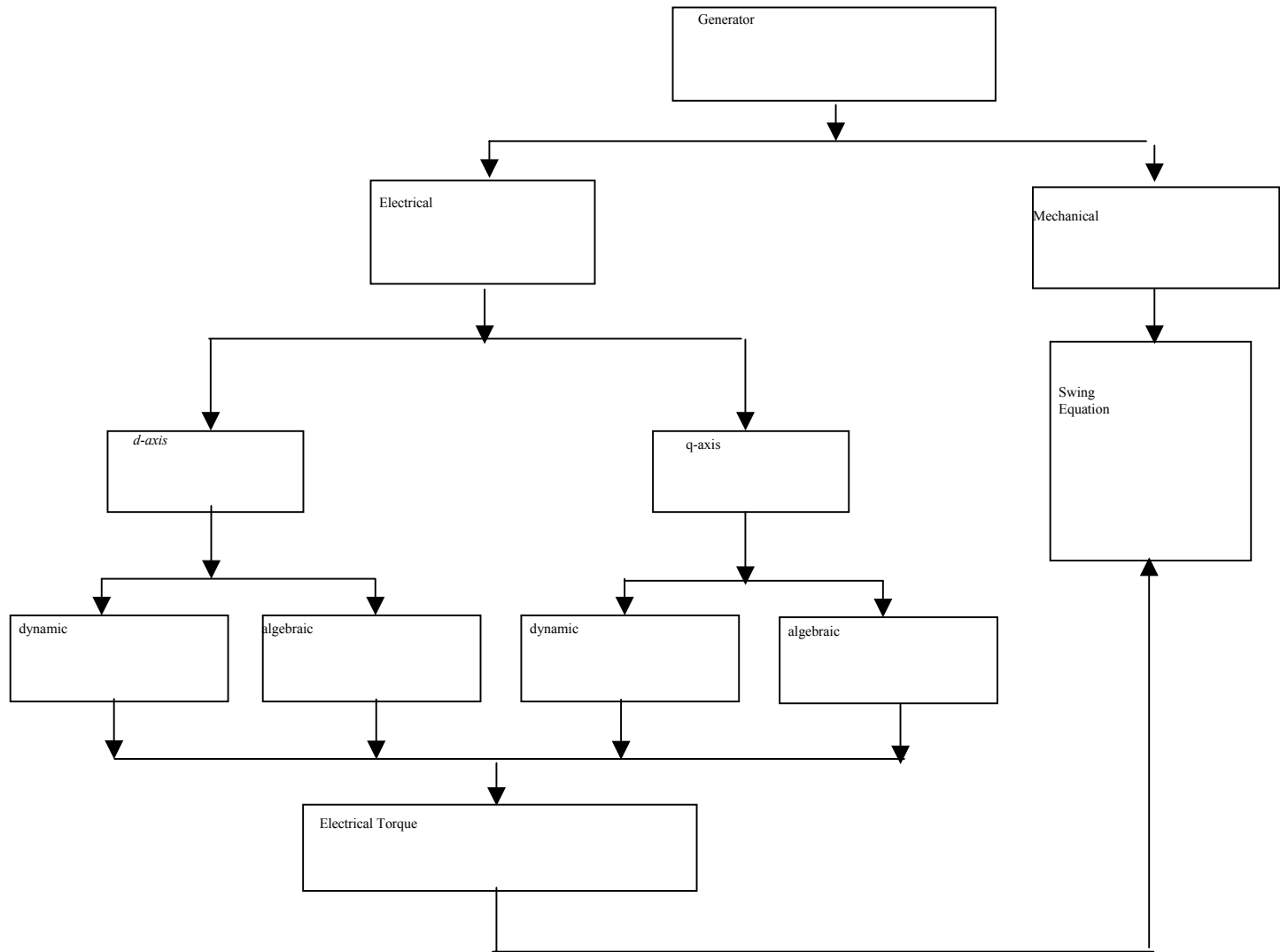
- Have redundant flight control surfaces, eg 17 instead of traditional 3 (aileron, elevator, rudder).
- Control reconfigurator distributes control effort amongst functioning control surfaces

Example 2: Power Systems

- Detect, locate fault + reconfigure generation







Modelling for FTC

- Nonlinear dynamical system, with state vector x , input vector u , output vector y , and fault signal vector f :

$$\dot{x} = f(x, u, m, t)$$

$$y = g(x, u, m, t)$$

Fault Detection and Isolation

- Requirement: design a filter to unambiguously detect each possible fault {Isidori, differential geometry...}
- Simpler problem: design a bank of filters with each customised toward detecting a specific fault {Mueller, svd}

Design of FTC system

- Start with fault detection filter, then use active control reconfiguration
- Various possibilities:
 - Switched controllers
 - Smoothly-scheduled controllers

Unknown Inp Obs [Hou & Mueller]

- plant

$$\dot{x}(t) = Ax(t) + Bu(t) + \sum_{i=1}^k L_i m_i(t)$$

$$y(t) = Cx(t)$$

- filter

$$\dot{w}(t) = H_1 w(t) + H_2 y(t) + H_3 u(t)$$

$$r(t) = H_4 w(t) + H_5 y(t)$$

Plant model

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 3 & 4 \\ 1 & 2 & 3 \\ 0 & 2 & 5 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 1 \\ -0.5 \\ 0.5 \end{bmatrix} m_1 + \begin{bmatrix} -3 \\ 1 \\ 0 \end{bmatrix} m_2$$

FDI filter #1

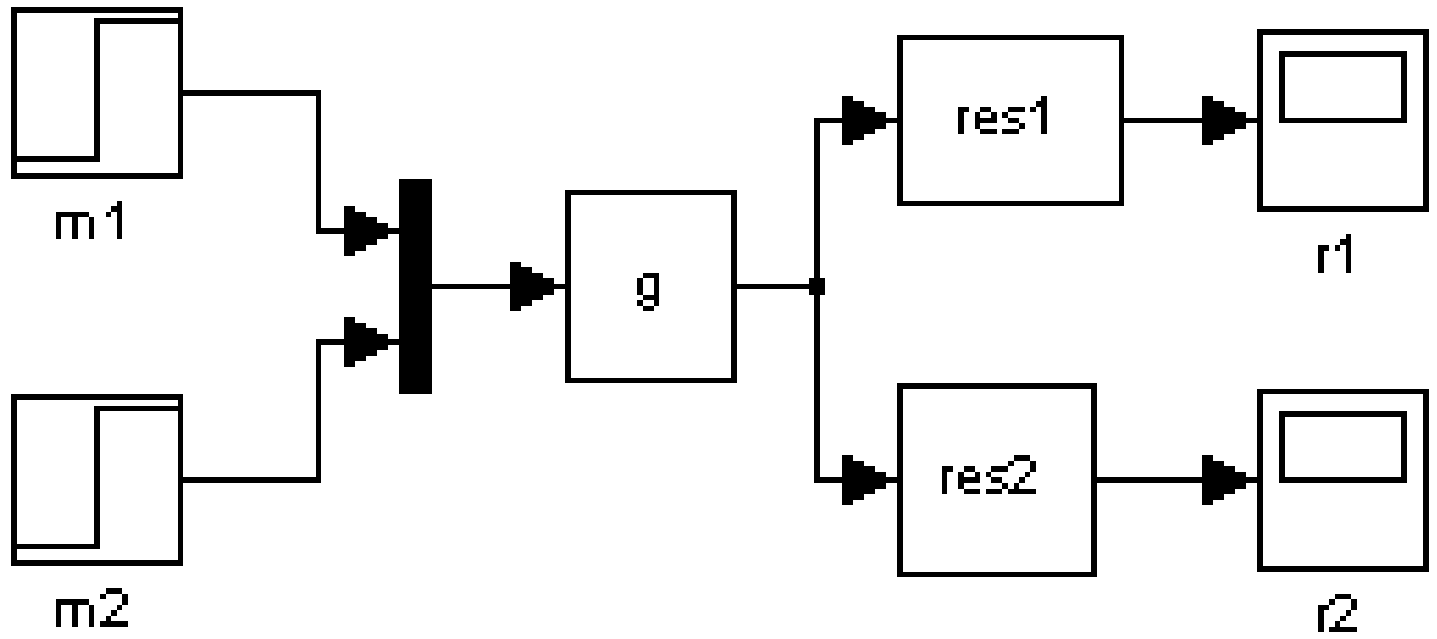
$$\dot{\eta} = (5 - \alpha)\eta + [2 \quad \alpha]y \quad \alpha > 5$$

$$r_1 = -\eta + [1 \quad 0]y$$

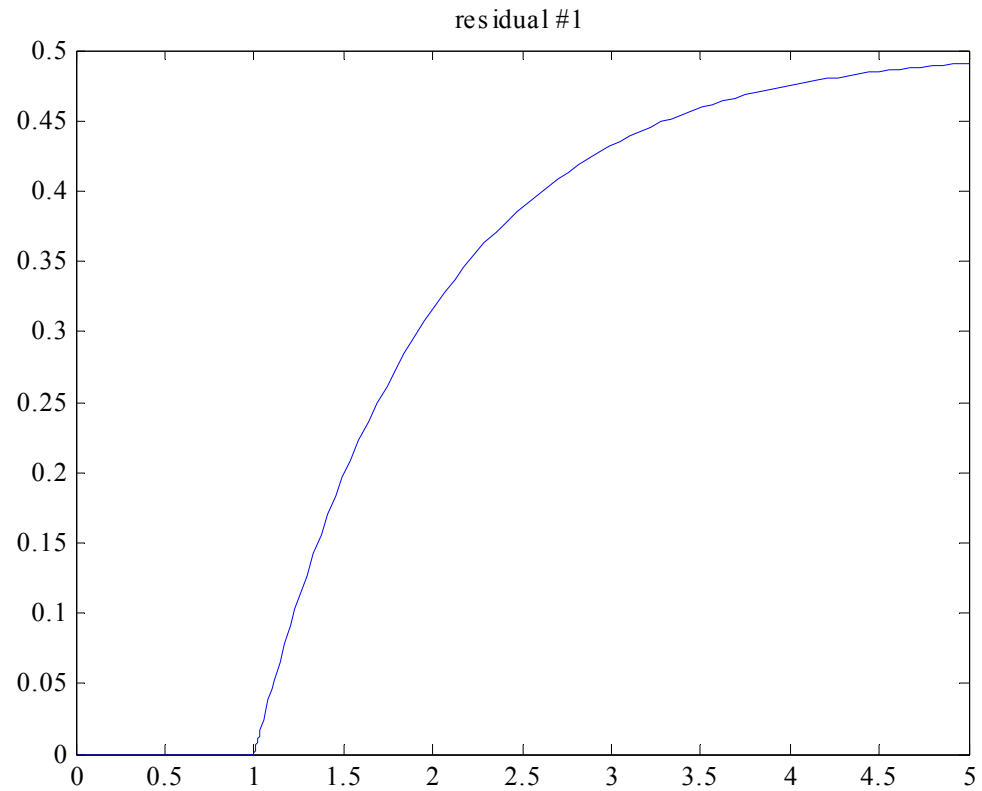
- FDI filter #2

$$\dot{\xi} = \begin{bmatrix} 2 & 3 - l_1 \\ 1 & 2 - l_2 \end{bmatrix} \xi + \begin{bmatrix} l_1 & 7 + l_1 \\ l_2 & 6 + l_2 \end{bmatrix} y$$

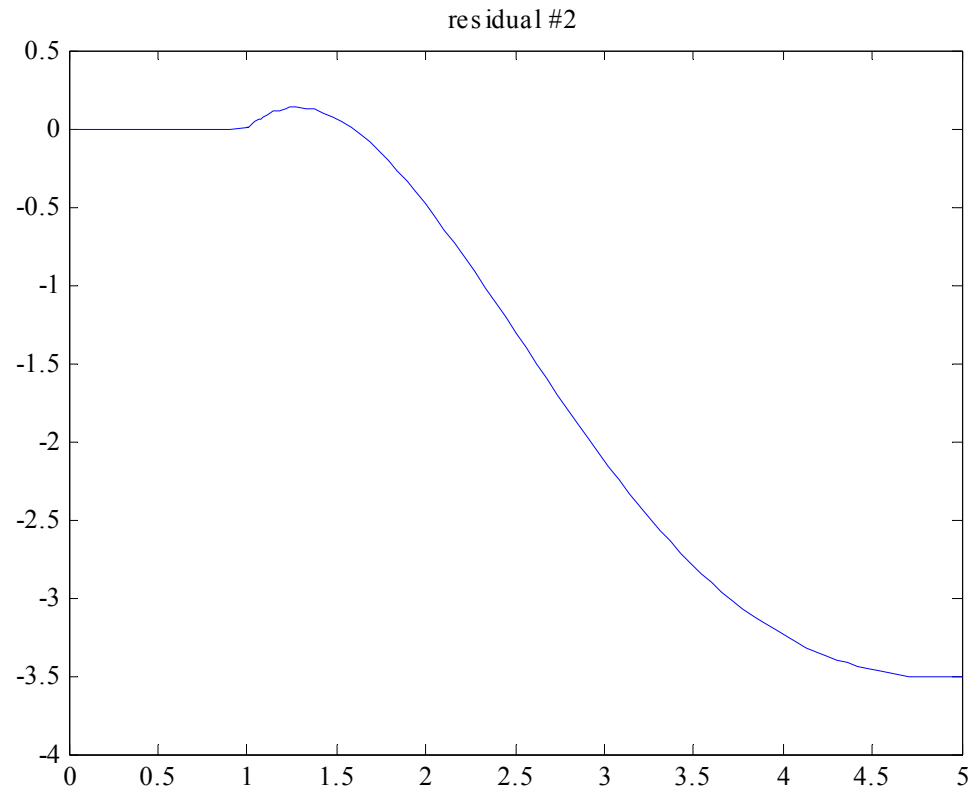
$$r_2 = \begin{bmatrix} 0 & -1 \end{bmatrix} \xi + \begin{bmatrix} 1 & 1 \end{bmatrix} y$$



Performance of filter #1



Performance of filter #2



Conclusions

- FTC remains largely an open problem, much research required (present theory only copes with very simple systems and is therefore not of any practical use).